## SEMICONDUCTOR PHYSICS

Semiconductors are the material, which have conductivity less than conductors and more than insulators.

For example:- Silicon and Germanium.

## TYPES OF SEMICONDUCTOR

## Intrinsic semiconductors:- These semiconductors are the

 purest and their conductivity is very low.2. Extrinsic semiconductors:- To increase the conductivity some impurity is added to the pure semiconductor, so that the conductivity increase. This process is known as doping.

These are of two types:-
i) N-type semiconductors:- When pentavalent impurity like phosphorus antimony or bismuth is added to pure semiconductor, one extra electron is added for every doped atom, so that the number of electrons will become more and it is called N -type semiconductors.
ii) P-type semiconductors:- When trivalent impurity like boron, aluminium is added to the pure semiconductor, one hole becomes free for every doped atom, so that the number of holes become more and it is called P-type semiconductors.

## PN-JUNCTION DIODE

When a P-type semiconductor is brought in contact with the N-type semiconductor, the resulting arrangement is called PN-Junction Diode.

In this, the electrons from N-type move to P-type and holes from P-type to N -type. The region in between $P$ and $N$ type is called depletion layer.

## Barrier potential:-

Minority carriers in P-type and N -type semiconductors namely electrons and holes respectively try to move towards the regions where they are in excess and so their number on both sides of depletion layer increases which produces a potential difference between the two sides of depletion layer called potential barrier.

## RECTIFIER

A rectifier is mainly a device which converts Alternating Current (AC) to Direct Current (DC)

Two types of rectifier:-
i) Half wave rectifier.
ii) Full wave rectifier.

## HALF WAVE RECTIFIER

The process of removing one-half the input signal to establish a DC Level is called Half Wave Rectification.

In Half Wave Rectifier only half of the wave i.e. positive half cycle appears at the output and negative half cycle is suppressed.


## WORKING

The AC supply to be rectified is given through a transformer. The transformer is used to step-up or step-down. During positive half cycle of input AC voltage the terminal $A$ is positive so that diode is forward bias and current appears across $R_{L}$.

During negative half cycle polarity changes and diode reverse bias and no current flows.

## DISADVANTAGES

i) The output is low because a.c. supply delivers power for half cycle only.
ii) The output contains a lot of ripples.

## FULL WAVE RECTIFIER

To overcome the limitation of half wave rectifier, full wave rectifier is used in which output appears for both the half cycle.


## WORKING

When $A C$ is switched on, the ends $A$ and $B$ become +ve and -ve during +ve half cycle, so that diode $D_{1}$ being forward biased and current will appears across the $R_{L}$. During -ve half cycle $B$ is +ve and $A$ is -ve, so that diode $D_{2}$ being forward biased and current will appears through $R_{L}$. Hence, both the half cycles are utilized for the output.

## ADVANTAGES

The output and efficiency is high, because AC supply delivers power during both the half cycles.

POLYMERS AND PLASTICS

## POLYMERS :

Polymers are the substances with very high molecular masses and each molecule of which consists of a large number of simple molecules joined by covalent bond. MONOMER :
The repeating unit present in a polymer is known as Monomer POLYMERISATION:
the process by which monomers are converted into polymers is called

## TYPES OF POLYMERS

There are mainly two types of polymers

- Natural : cotton, silk, wood, leather...
-Synthetic : plastics, nylon, latex...


## FOR EXAMPLE, POLYTHENE IS OBTAINED FROM A LARGE NUMBER OF ETHENE MOLECULES BY POLYMERISATION.

$$
\begin{aligned}
& n\left(\mathrm{CH}_{2}=\mathrm{CH}_{2}\right) \quad 3 / 43 \frac{23}{4} / \mathbb{B} \quad\left(\mathrm{CH}_{2}-\mathrm{CH}\right)_{n} \\
& \text { (Monomer) high pressure }
\end{aligned}
$$

## THERMOPLASTICS

- Thermoplastics soften when heated and can be moulded into required shapes when in this state. They will harden again on cooling. By heating and cooling, they can be softened and heated over and over again.


## THERMOSETTING PLASTICS

- Will only mould once.
- Strong primary bonds are connected by strong covalent bonds.
- Cross-link process (curing) formed by heat and pressure.
- Non-reversible structure cannot be softened by heating.
- Phenol formaldehyde. Hard and brittle, 'Bakelite' has been used for electrical fittings and saucepan handles.
- Urea formaldehyde. Good electrical and thermal properties and used for electrical fittings and door handles.


## METHODS FOR MAKING POLYMERS

## ADDITION POLYMERIZATION AND CONDENSATION POLYMERIZATION

## Addition polymerization:

 monomers react to form a polymer without net loss of atoms.Most common form: free radical chain reaction of ethylenes


## Two main synthetic approaches

- Addition polymerization
- Simply adding monomers together synthetic plastics
- Condensation polymerization
- Combination by exclusion of a small molecule (usually water) extensively used by nature


## Condensation polymerization

Condensation polymerization: the polymer grows from monomers by splitting off a small molecule such as water or carbon dioxide.
Example: Nylon-66
. NYLON-66:-
It is prepared by condensation polymerization of hexamethylenediamine and Adipic acid.


The fibres of Nylon-66 have very high tensile strength. They are quite tough and resistant to abrasion.

## Uses:

It is used in making bristles of toothbrush, socks, sheets, ropes, etc and also in textile industries

## Uses of Polymers

- Polymers are incorporated into nearly every aspect of daily life
- Entertainment
- Sports
- Clothes
- Hobbies/Toys
- Household products
- Automotive


## IN DAILY LIFE:

Polymers are the backbone of the modern civilization. The polymers are commonly used in our day to day life example cars, bikes, scooters, furniture, clothing, medical equipments, plastic ware, etc. The article of common use such as radio, televisions, mobiles, sun glasses, bottles, buckets, packaging containers, toys, electrical switches, kitchen wares (bowl, mugs, saucers, plates, trays, etc) and other decorative articles are made up of polymers.

## STATISTICS

Definations: Statistics ; Measure of central tendency

- Defination of statistics: statistics may be defined as the science of collection, organization, analysis and interpretation of numerical data.
- Measures of Central Tendency: An average is called a measure of central tendency, because it tends to lie centrally with the values of the variable arranged according to magnitude.


## Arithmetic Mean(A.M.):

The arithmetic mean of an individual series is defined as the quotient of the sum of all the values of the variable by the total number of items.

$$
\bar{x}=\frac{1}{n} \sum_{i=1}^{n} x_{i}
$$

## Example 1

Example : The blood pressure of seven middle aged men were as follows:
$151,124,132,170,146,124$ and 113.

$$
\bar{x}=\frac{(151+124+132+170+146+124+113)}{7}
$$

The mean is

$$
=137.14
$$

## In case of discrete frequency distribution A.M. is calculated as:

$$
\begin{aligned}
\text { A.M. }(\mathrm{X})= & \sum\left(\mathrm{f}_{\mathrm{i}} \mathrm{x}_{\mathrm{i}}\right) / \sum \mathrm{f}_{\mathrm{i}} \\
& \mathrm{OR} \sum(\mathrm{fx}) / \sum \mathrm{f}
\end{aligned}
$$

Where $f_{i}$ is the frequency of $x_{i}(1 \leq I \leq n)$

## Example2



## For Grouped or continuous frequency

 distribution, Arithmatic mean is calculated as:
## Arithmatic Mean $=A+\sum \mathrm{f}_{\mathrm{i}} \mathrm{u}_{\mathrm{i}} \quad{ }^{*} \mathrm{~h}$ $\sum \mathrm{f}_{\mathrm{i}}$

This method is called STEP DEVIATION METHOD

## EXAMPLE 3

Calculate the Arithmetic mean of the marks scored by the students of a class in a class test from the following data :

| Marks | Number of <br> students | Mid Point $\left(x_{i}\right)$ | $u i=(x i-A) / h$ | fiui |
| :---: | :---: | :---: | :---: | :---: |
| $0-10$ | 12 | 5 | -2 | -24 |
| $10-20$ | 18 | 15 | -1 | -18 |
| $20-30$ | 27 | $\mathrm{~A}=25$ | 0 | 0 |
| $30-40$ | 20 | 35 | 1 | 20 |
| $40-50$ | 17 | 45 | 2 | 34 |
| $50-60$ | 6 | 55 | 3 | 18 |
| Total | 100 |  |  | 30 |

By step Deviation method, Arithmatic mean $=A+(\Sigma f i u i / \Sigma f i) * h$

$$
=25+(30 / 100) * 10=28
$$

## Median :

The median of a statistical series is defined as the size of the middle most item (or the A.M. of two middle most items), provided the items are in the order of magnitude.
For an individual series, to find median we proceed as follow:
(a) Arrange the observations in ascending or descending order of magnitude.
(b) If n is odd; then median $=(\mathrm{n}+1 / 2)^{\text {th }}$ observation.

If n is even; them median $=$ A.M. of $(\mathrm{n} / 2)^{\text {th } \&}$
( $\mathrm{n} / 2$ ) $+1^{\text {th }}$ observation.

## Framnlo 1.

## Find the median of the values:

$\begin{array}{llllllll}31 & 38 & 27 & 28 & 36 & 25 & 35 & 40\end{array}$
Sol: We arrange the values in ascending order

$$
\begin{array}{llllllll}
25 & 27 & 28 & 31 & 35 & 36 & 38 & 40 \\
\mathrm{n}=8 \text { (even); }
\end{array}
$$

Median $=$ A.M. of $(8 / 2)^{\text {th } \&}(8 / 2)+1^{\text {th }}$ observations

$$
=(31+35) / 2=33
$$

# In case of discrete frequency 

 distribution Median is calculated as:- Step I: Find the cumulative frequency (C.F.).
- Step 2: Find $N / 2$ where $N=\sum f_{i}$
- Step 3: See the C.F. just greater than N/2.

Step 4: The value of $x$ corresponding to C.F. just greater than $\mathrm{N} / 2$ is median.

## Example 2:

Calculate the Median of the following frequency distribution :

| X | f | c.f. |
| :---: | :---: | :---: |
| 1 | 8 | 8 |
| 2 | 10 | 18 |
| 3 | 11 | 29 |
| 4 | 16 | 45 |
| 5 | 20 | 65 |
| 6 | 25 | 90 |
| 7 | 15 | 105 |
| 8 | 9 | 114 |
| 9 | $\mathrm{~N}=120$ | 120 |

Here N is 120; N/2 is 60; C.F. just greater than N/2 is 65; So corresponding value of $x$ ' 5 ' is median.

## For Grouped or continuous frequency distribution, Median is calculated as:

- Step I: Find the cumulative frequency (C.F.).
- Step 2: Find $N / 2$ where $N=\sum f_{i}$
- Step 3: The class corresponding to C.F. just greater than $\mathrm{N} / 2$ is median class and the value of the median is calculated by formula:

Median $=1+((\mathrm{N} / 2-\mathrm{F}) / \mathrm{f}) * \mathrm{~h}$
Where $\mathrm{l}=$ lower limit of median class
$\mathrm{F}=\mathrm{C} . \mathrm{F}$. of class preceding the median class
$f$ is the frequency of median class
$h$ is the width of median class.

## Example 3

## Calculate the median from the following distribution:

| Class | Freuency | Cumative frequency |
| :---: | :---: | :---: |
| $5-10$ | 5 | 5 |
| $10-15$ | 6 | $11(\mathrm{~F})$ |
| $15-20$ (Median class) | $15(\mathrm{f})$ | $26(\mathrm{C} . \mathrm{F}$. just greater than $\mathrm{N} / 2)$ |
| $20-25$ | 10 | 36 |
| $25-30$ | 5 | 41 |
| $30-35$ | 2 | 45 |
| $35-40$ | $\mathrm{~N}=49$ | 49 |
| $40-45$ | $\mathrm{~N} / 2=24.5$ | C.F. just greater than $\mathrm{N} / 2$ is 26 |
|  | Median $=1+((\mathrm{N} / 2-\mathrm{F}) / \mathrm{f}) * \mathrm{~h}$ |  |
| Here $\mathrm{N}=49$ |  |  |
| Corresponding class $15-20$ is median class | Mer\| |  |
| Median $=15+(24.5-11) / 15 * 5=19.5$ |  |  |

## MODE

- The mode of a distribution of the variable is that value of the variable for which the frequency is maximum.
- In case of an individual series, mode is calculated as by counting the number of times the various values repeat themselves and the value which occurs maximum no. of times is the modal value.


## In case of discrete frequency distribution mode is calculated as:

For discrete frequency distribution, generally mode is calculated by finding the value for which frequency is maximum.

## Example 2

## Find the mode of the following distribution:

| Size in inches | No of shirts sold |
| :---: | :---: |
| 30 | 8 |
| 32 | 17 |
| 34 | 30 |
| 36 | 35 |
| 38 | 18 |
| 40 | 7 |
| 42 | 3 |
| 35 shirts of size 36 have the maximum sale. So mode of distribution is "36". |  |

# For grouped or continuous frequency distribution mode is 

 calculates as:To find the mode of continuous frequency distribution, we follow the following steps:

STEP 1: Determine the class of maximum frequency, this class is modal class.

STEP 2: Determine the value of mode by applying the formula:
Mode $=1+\left(f-f_{1} / f-f_{1}-f_{2}\right) * h$
Where $l$ is the lower limit of modal class
$f$ is the frequency of modal class
$h$ is the width of modal class
$\mathrm{f}_{1}$ is the frequency of class preceding the modal class
$\mathrm{f}_{2}$ is the frequency of class following the modal class

## Example 3

Calculate the mode from the following data:

| Rent (in Rs.) | No. of houses |
| :---: | :---: |
| $20-40$ | 6 |
| $40-60$ | 9 |
| $60-80$ | 11 |
| $80-100$ | $14\left(\mathrm{f}_{1}\right)$ |
| $100-120$ (Modal class) | $20(\mathrm{f})$ |
| $120-140$ | $15\left(\mathrm{f}_{2}\right)$ |
| $140-160$ | 10 |
| Highest frequency is 20 | Hence Modal class is $100-120$ |
| Mode $=\mathrm{l}+\left(\mathrm{f}-\mathrm{f}_{1} / \mathrm{f}-\mathrm{f}_{1}-\mathrm{f}_{2}\right) * \mathrm{~h}$ |  |
| Here $\mathrm{l}=100 ; \mathrm{h}=20 ; \mathrm{f}=20 ; \mathrm{f}_{1}=14 ; \mathrm{f}_{2}=15$ |  |
| Mode $=100+(20-14) /(2 * 20-14-15) * 20=110.91$ |  |

## Measures of dispersion

- Mean Deviation: It is defined as the A.M. of the absolute deviations of all the values taken from any central value.
- Standard Deviation: The standard deviation of a statistical data is defined as the positive square root of the A.M. of the squared deviations of items from the A.M. of the series under consideration.


## For individual series Mean doviation is calculatod ac.

Mean Deviation $(x)=\sum\left|x_{i}-x\right|$
n
Mean Deviation $($ Median $)=\Sigma \mid \mathrm{x}_{\mathrm{i}}-$ Median
Cofficient of Mean Deviation (x) $\stackrel{n}{=}$ M.D.(X) X
Cofficient of Mean Deviation $($ Median $)=$ M.D.(Medain)/Median

## Example 1

Calculate the mean deviation about mean and its coefficient for the following data: 21232528303246384846

| S.No. | $\mathbf{X i}$ | $\mathbf{x i}-\mathbf{x}$ | $\left\|\mathbf{x}_{\mathbf{i}}-\mathbf{x}\right\|$ |
| :---: | :---: | :---: | :---: |
| 1 | 21 | -12.7 | 12.7 |
| 2 | 23 | -10.7 | 10.7 |
| 3 | 25 | -8.7 | 8.7 |
| 4 | 28 | -5.7 | 5.7 |
| 5 | 30 | -3.7 | 3.7 |
| 6 | 32 | -1.7 | 1.7 |
| 7 | 46 | 12.3 | 12.3 |
| 8 | 48 | 4.3 | 4.3 |
| 9 | 46 | 14.3 | 14.3 |
| 10 | Mean $=$ | M.D. $=86.4 / 10=8.64$ | Coeff. $=8.64 / 33.7=26$ |
| $337 / 10=33.7$ |  |  | 12.3 |

## For frequency distribution \& Grouped Data M.D.is calculated as:

Mean Deviation ( x ) $=\sum \mathrm{f}_{\mathrm{i}} \mid \mathrm{x}_{\mathrm{i}}-\mathrm{x}$
Mean Deviation (Median ) ${ }^{n}=\sum f_{i} \mid x_{i}-$ Median $\mid$
N

## Example 2

Calculate the mean deviation about mean and its coefficient for the following frequency distribution:

| $\mathbf{X}$ | $\mathbf{f}$ | $\mathbf{f x}$ | $\mathbf{X}-\mathbf{x}$ | $\|\mathbf{x}-\mathbf{x}\|$ | $\mathbf{f}\|\mathbf{x}-\mathbf{x}\|$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 5 | 8 | $\mathbf{4 0}$ | -4 | $\mathbf{4}$ | $\mathbf{3 2}$ |
| 7 | 6 | 42 | -2 | $\mathbf{2}$ | $\mathbf{1 2}$ |
| 9 | 2 | $\mathbf{1 8}$ | $\mathbf{0}$ | $\mathbf{0}$ | $\mathbf{0}$ |
| 10 | 2 | $\mathbf{2 0}$ | $\mathbf{1}$ | $\mathbf{1}$ | $\mathbf{2}$ |
| 12 | 2 | 24 | $\mathbf{3}$ | $\mathbf{3}$ | $\mathbf{6}$ |
| 15 | 6 | $\mathbf{9 0}$ | $\mathbf{6}$ | $\mathbf{6}$ | $\mathbf{3 6}$ |

## For Individual series \& frequency distribution Standard Deviation is calculated as:

$$
\text { S.D.(Individual series) }=\sqrt{\sum_{i=1}^{i=n}(x i-x)^{2} / n}
$$

Where $x_{i}$ are the values of variable under consideration.
S.D. (For Discrete Frequency distribution):

$$
\sqrt{\sum_{i=1}^{i=n} f i\left(x i-\mathrm{x}^{12} / \mathrm{N}\right.}
$$

Where $N$ is the sum of all the frequencies.

## Example 1

Find the S.D. and C.V. for the following data:
4,6,10,12,18

| S.No. |
| :--- |
| 1 |

## Example 2

## Calculate the S.D. and C.V. for the following

| X | f | fx | X - X | $(x-x)^{2}$ | $\mathrm{f}(\mathrm{x}-\mathrm{x})^{\mathbf{2}}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 5 | 12 | 60 | -23 | 529 | 6348 |
| 15 | 18 | 270 | -13 | 169 | 3042 |
| 25 | 27 | 675 | -3 | 9 | 243 |
| 35 | 20 | 700 | 7 | 49 | 980 |
| 45 | 17 | 765 | 17 | 289 | 4913 |
| 55 | 6 | 330 | 27 | 729 | 4374 |
|  | $\sum \mathrm{f}=100$ | $\sum \mathrm{fx}=2800$ |  |  | $\sum \mathrm{f}(\mathrm{x}-\mathrm{x})^{\mathbf{2}=19900}$ |
| Mean $=2800 / 100=28$ |  |  |  |  |  |
| S.D. $=\sqrt{\sum_{i=1}^{i=n} f i(x i-\bar{x})^{2}} / \mathrm{N}$ |  |  |  | S.D. $=V 19900 / 100=14.11$ |  |
| C.V. $=$ S.D. $/$ Mean * $100=50.39 \%$ |  |  |  |  |  |

## For Grouped data S.D. is calculated

 as:S.D. $=\sqrt{ } \sum \mathrm{f}_{\mathrm{i}}\left(\mathrm{u}_{\mathrm{i}}\right)^{2} / \mathrm{N}-\left(\sum \mathrm{f}_{\mathrm{i}} \mathrm{u}_{\mathrm{i}} / \mathrm{N}\right)^{2} / \mathrm{N}^{*} \mathrm{~h}$

Where $u_{i}=x_{i}-A$ and $N$ is the sum of
frequency.
h

## Example 3

Find the S.D. \& C.V. for the following data:

| class | $\mathbf{f}$ | $\mathbf{x}$ | $\mathbf{U}=\mathbf{x}-\mathbf{A} / \mathbf{h}$ | $\mathbf{f u}$ | $\mathbf{u}^{\mathbf{2}}$ | $\mathbf{f u}^{\mathbf{2}}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $0-5$ | 20 | $\mathbf{2 . 5}$ | $-\mathbf{4}$ | $\mathbf{- 8 0}$ | $\mathbf{1 6}$ | $\mathbf{3 2 0}$ |
| $5-10$ | 24 | $\mathbf{7 . 5}$ | $\mathbf{- 3}$ | $-\mathbf{- 7 2}$ | $\mathbf{9}$ | $\mathbf{2 1 6}$ |
| $10-15$ | 32 | $\mathbf{1 2 . 5}$ | $-\mathbf{2}$ | $\mathbf{- 6 4}$ | $\mathbf{4}$ | $\mathbf{1 2 8}$ |
| $15-20$ | 28 | $\mathbf{1 7 . 5}$ | $\mathbf{- 1}$ | $\mathbf{- 2 8}$ | $\mathbf{1}$ | $\mathbf{2 8}$ |
| $20-25$ | 20 | $\mathbf{2 2 . 5}$ | $\mathbf{0}$ | $\mathbf{0}$ | $\mathbf{0}$ | $\mathbf{0}$ |
| $25-30$ | 16 | $\mathbf{2 7 . 5}$ | $\mathbf{1}$ | $\mathbf{1 6}$ | $\mathbf{1}$ | $\mathbf{1 6}$ |
| $30-35$ | 34 | $\mathbf{3 2 . 5}$ | $\mathbf{2}$ | $\mathbf{6 8}$ | $\mathbf{4}$ | $\mathbf{1 3 6}$ |
| $35-40$ | 10 | $\mathbf{3 7 . 5}$ | $\mathbf{3}$ | $\mathbf{3 0}$ | $\mathbf{9}$ | $\mathbf{9 0}$ |
| $40-45$ | 16 | $\mathbf{4 2 . 5}$ | $\mathbf{4}$ | $\mathbf{6 4}$ | $\mathbf{1 6}$ | $\mathbf{2 5 6}$ |
|  | $\sum \mathbf{f}=\mathbf{2 0}$ |  |  | $\sum \mathbf{f u}=-\mathbf{6 6}$ |  | $\sum \mathrm{fu}^{2}=\mathbf{1 1 9 0}$ |
|  | $\mathbf{0}$ |  |  |  |  |  |

Mean $=A+\sum f u / \sum f * h=20.85$ S.D. $=\sqrt{ } \sum f_{i}\left(u_{i}\right)^{2} / N-\left(\sum f_{i} u_{i} / N\right)^{2} / N * h=$ 12.1
C.V. $=$ C.V. $=$ S.D. $/$ Mean $* 100=58.03 \%$

## OTHER FORMULAS (S.D.)

- Cofficient of S.D. $=$ S.D./Mean
- $\underline{\text { Cofficient of variation }}=($ S.D. $/$ Mean $) * 100$
- Variance $=$ Square of S.D.


## Rank Correlation Coefficient:

Rank Coorelation Coefficient is given by the formula:

$$
\begin{array}{r}
r=1-6 \sum d^{2} \\
n\left(n^{2}-1\right)
\end{array}
$$

Where $\underline{n}$ is no. of items
d is the difference of ranks.

## Example 1

Find the coefficient of rank correlation for the following data:

| x | y | R1 | R2 | d=R1-R2 | $\mathrm{d}^{2}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 56 | 15 | 3 | 2 | 1 | 1 |
| 58 | 12 | 4 | 1 | 3 | 9 |
| 62 | 16 | 5 | 3 | 2 | 4 |
| 72 | 17 | 7 | 4 | 3 | 9 |
| 54 | 19 | 2 | 5 | -3 | 9 |
| 52 | 20 | 1 | 6 | -5 | 25 |
| 71 | 21 | 6 | 7 | -1 | 1 |
| 90 | 22 | 9 | 8 | 1 | 1 |
| 81 | 23 | 8 | 9 | -1 | 1 |
| 92 | 24 | 10 | 10 | 0 | 0 |
|  |  |  |  |  | $\sum \mathrm{d}^{2}=60$ |
| $r=1-(6 * 60) / 10(100-1)=0.64$ |  |  |  |  |  |

## Crearands?

Seven Competitors in a music competition are ranked by the judges x \& y in the following order. What is the degree of agreement between the judges. Also find the coefficient of correlation.

| S.No. | Competitors | $\mathbf{R 1}$ | $\mathbf{R 2}$ | $\mathbf{d =} \mathbf{R 1} \mathbf{- R 2}$ | $\mathbf{d}^{\mathbf{2}}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | A | 2 | 1 | $\mathbf{1}$ | $\mathbf{1}$ |
| 2 | B | 1 | 3 | $\mathbf{- 2}$ | $\mathbf{4}$ |
| 3 | C | 4 | 2 | $\mathbf{2}$ | $\mathbf{4}$ |
| 4 | D | 3 | 4 | $\mathbf{- 1}$ | $\mathbf{1}$ |
| 5 | E | 5 | 5 | $\mathbf{0}$ | $\mathbf{0}$ |
| 6 | F | 7 | 6 | $\mathbf{1}$ | $\mathbf{1}$ |
| 7 | G | 6 | 7 | $\mathbf{- 1}$ | $\mathbf{1}$ |
|  |  |  |  |  | $\sum \mathbf{d}^{2}=\mathbf{1 2}$ |

$\mathrm{r}=1-(72 / 7 * 48)=.7857$ (Agreement between the judges is high)

